

1.  $|\vec{a} \times \vec{b}| + (\vec{a} \cdot \vec{b})^2 =$   
 (A)  $|\vec{a}|^2 + |\vec{b}|^2$  (B)  $|\vec{a}|^2 - |\vec{b}|^2$   
 (C)  $|\vec{a}|^2 |\vec{b}|^2$  (D) None of these

2. The area of a triangle whose vertices are, A (1, -1, 2), B (2, 1, -1) and C (3, -1, 2) is :  
 (A) 13 (B)  $\sqrt{13}$   
 (C) 6 (D)  $\sqrt{6}$

3. If  $\vec{a}$  &  $\vec{b}$  are two non-zero vectors, then the component of  $\vec{b}$  along  $\vec{a}$  is  
 (A)  $\frac{(\vec{a} \cdot \vec{b}) \vec{b}}{\vec{a} \cdot \vec{a}}$  (B)  $\frac{(\vec{a} \cdot \vec{b}) \vec{a}}{\vec{a} \cdot \vec{a}}$   
 (C)  $\frac{(\vec{a} \cdot \vec{b}) \vec{b}}{\vec{a} \cdot \vec{b}}$  (D)  $\frac{(\vec{a} \cdot \vec{b}) \vec{a}}{\vec{a} \cdot \vec{a}}$

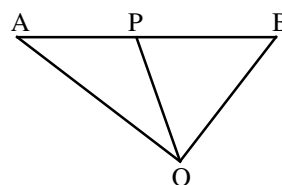
4. If  $\vec{a} + \vec{b} + \vec{c} = 0$ , then which relation is correct .  
 (A)  $\vec{a} = \vec{b} = \vec{c} = 0$   
 (B)  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a}$   
 (C)  $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} = \vec{c} \times \vec{a}$   
 (D) None of these

5. If ABCDEF is a regular hexagon and  $\vec{AB} + \vec{AC} + \vec{AD} + \vec{AE} + \vec{AF} = \lambda \vec{AD}$ , then  $\lambda =$   
 (A) 2 (B) 3  
 (C) 4 (D) 6

6. If O be the circumcentre and O' be the orthocentre of a triangle ABC, then

- $\vec{OA} + \vec{OB} + \vec{OC} =$   
 (A)  $2 \vec{OO'}$  (B)  $2 \vec{O'O}$   
 (C) (D)  $\vec{O'O}$

7. If in the given fig.  $\vec{OA} = \vec{a}$ ,  $\vec{OB} = \vec{b}$  and  $AP : PB = m : n$ , then  $\vec{OP} =$



- (A)  $\frac{m\vec{a} + n\vec{b}}{m+n}$  (B)  $\frac{n\vec{a} + m\vec{b}}{m+n}$   
 (C)  $m\vec{a} - n$  (D)

8. If  $\vec{a} = 2\hat{i} + 2\hat{j} + 3\hat{k}$ ,  $\vec{b} = 3\hat{i} + \hat{j}$  and  $\vec{c} = 3\hat{i} + \hat{j}$ , then  $\vec{a} + t\vec{b}$  is perpendicular to  $\vec{c}$  if  $t =$   
 (A) 2 (B) 4  
 (C) 6 (D) 8

9. The area of the parallelogram whose diagonals are,  $\vec{a} + \vec{b}$  and  $\vec{a} - \vec{b}$  is :  
 (A)  $10\sqrt{3}$  (B)  $5\sqrt{3}$   
 (C) 8 (D) 4

10.  $\vec{a} \cdot \{(\vec{a} + \vec{b}) \times (\vec{a} + \vec{c})\} =$   
 (A) 0  
 (B)  $[\vec{a} \vec{b} \vec{c}] + [\vec{a} \vec{c} \vec{b}]$   
 (C)  $[\vec{a} \vec{b} \vec{c}]$  (D) None of these

QUEST TUTORIALS

11. If the vectors  $\hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelopiped, then the volume of the parallelopiped is :  
 (A) 8 (B) 10  
 (C) 4 (D) 14
12.  $|(\vec{a} \times \vec{b}) \cdot \vec{c}| = |\vec{a}| |\vec{b}| |\vec{c}|$ , if :  
 (A)  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = 0$   
 (B)  $\vec{a} \cdot \vec{c} = \vec{b} \cdot \vec{c} = 0$   
 (C)  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c} = 0$   
 (D)  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c} = \vec{b} \cdot \vec{c} = 0$
13. If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$ , then  
 $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} =$   
 (A) 1 (B) 3  
 (C) - (D)
14. If the position vectors of the points A, B, C be  $\vec{a}, \vec{b}, 3\vec{c} - 2\vec{a}$  respectively then the points A, B, C are :  
 (A) Collinear (B) Non-collinear  
 (C) Form a right angled triangle  
 (D) None of these
15. If  $\vec{a}$  &  $\vec{b}$  are the position vectors of A & B respectively, then the position vector of a point C on AB produced such that  $\vec{OC} = 3\vec{AB}$  is :  
 (A)  $3\vec{a} - \vec{b}$  (B)  $3\vec{a} - 2\vec{b}$   
 (C)  $3\vec{a} - 2\vec{b}$  (D)  $3\vec{a} - 2\vec{b}$
16. The position vectors of the points A, B & C are  $\vec{a}, \vec{b} + \vec{c}$  and  $\vec{c} + \vec{a}$  respectively. The vector area of the  $\Delta ABC = \pm \frac{1}{2}$ , where  $\vec{a} =$   
 (A)  $\hat{i} - \hat{j} + \hat{k}$   
 (C)  $\hat{i} + \hat{j} - \hat{k}$  (D)  $\hat{i} + \hat{j} + \hat{k}$
17. If  $\vec{a} = (1, -1, 1)$  &  $\vec{b} = (-1, -1, 0)$ , then the vector satisfying,  $\vec{a} \times \vec{c} = \vec{b}$  &  $\vec{c} \cdot \vec{a} = 1$ , is :  
 (A) (1, 0, 0) (B) (0, 0, 1)  
 (C) (0, -1, 0) (D) None of these
18. If  $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} \neq 0$ , then for some scalar k :  
 (A)  $\vec{a} + \vec{b} = k\vec{c}$  (B)  $\vec{a} + \vec{c} = k\vec{b}$   
 (C)  $\vec{a} + \vec{c} = k\vec{a}$  (D) None of these
19. P is the point of intersection of the diagonals of the parallelogram ABCD. If O is any point, then  $\vec{OP}$  is :  
 (A)  $\vec{OP}$  (B)  $2\vec{OP}$   
 (C)  $3\vec{OP}$  (D)  $4\vec{OP}$
20. A unit vector in the xy-plane which is perpendicular to  $4\hat{i} - 3\hat{j} + \hat{k}$  is :  
 (A)  $\frac{\hat{i} + \hat{j}}{\sqrt{2}}$  (B)  $\frac{1}{5}(3\hat{i} + 4\hat{j})$   
 (C)  $\frac{1}{5}(3\hat{i} - 4\hat{j})$  (D) None of these
21. If the position vectors of the points

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A, B, C, D be  $2\hat{i} + 3\hat{j} + 5\hat{k}$ ,

$\hat{i} + 2\hat{j} + 3\hat{k}$ ,  $-5\hat{i} + 4\hat{j} - 2\hat{k}$  and

$\hat{i} + 10\hat{j} + 10\hat{k}$  respectively, then :

(A)  $\vec{AB} = \vec{CD}$  (B)  $\vec{AB} \parallel \vec{CD}$

(C)  $\vec{AB} \perp$  (D) None of these

22. Let  $\vec{a} =$  be a vector which makes an angle of  $120^\circ$  with a unit vector

. Then the unit vector ( + ) is :

(A) (B)  $-\frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j}$

(C)  $\frac{1}{2}\hat{i} + \frac{\sqrt{3}}{2}\hat{j}$  (D)  $\frac{\sqrt{3}}{2}\hat{i} - \frac{1}{2}\hat{j}$

23. The points with position vectors,  $60\hat{i} + 3\hat{j}$ ,  $40\hat{i} - 8\hat{j}$ ,  $a\hat{i} - 52\hat{j}$  are collinear, if  $a =$

(A) - 40 (B) 40  
(C) 20 (D) None of these

24. If the scalar product of the vector,  $\hat{i} + \hat{j} + \hat{k}$  with a unit vector parallel to the sum of the vectors,  $2\hat{i} + 4\hat{j} - 5\hat{k}$  &  $\lambda\hat{i} + 2\hat{j} + 3\hat{k}$  be 1, then  $\lambda =$

(A) 1 (B) -1  
(C) 2 (D) -2

25. If  $\vec{a}$ , , are three non-coplanar vectors and are defined by the relations ,

$$\vec{p} = \frac{\vec{b} \times \vec{c}}{[\vec{a} \vec{b} \vec{c}]}, \vec{q} = \frac{\vec{c} \times \vec{a}}{[\vec{a} \vec{b} \vec{c}]}, \vec{r} = \frac{\vec{a} \times \vec{b}}{[\vec{a} \vec{b} \vec{c}]}$$

then,  $(\vec{a} + \vec{b}) \cdot \vec{p} + (\vec{b} + \vec{c}) \cdot \vec{q} + (\vec{c} + \vec{a}) \cdot \vec{r}$

is equal to :

(A) 0 (B) 1  
(C) 2 (D) 3

26. The unit normal vector to the line joining  $\hat{i} - \hat{j}$  &  $2\hat{i} + 3\hat{j}$  and pointing towards the origin is :

(A)  $\frac{4\hat{i} - \hat{j}}{\sqrt{17}}$  (B)  $\frac{-4\hat{i} + \hat{j}}{\sqrt{17}}$

(C)  $\frac{2\hat{i} - 3\hat{j}}{\sqrt{13}}$  (D)  $\frac{-2\hat{i} + 3\hat{j}}{\sqrt{13}}$

27. The position vector of a point C w.r.t. B is  $\hat{i} + \hat{j}$  & that of B w.r.t. A is  $\hat{i} - \hat{j}$ . The position vector of C w.r.t. A is :

(A)  $2\hat{i}$  (B)  $2\hat{j}$

(C)  $-2\hat{j}$  (D)  $2\hat{i}$

28. A unit vector perpendicular to the plane determined by the points,  $\frac{1}{2}\hat{i} + \frac{1}{2}\hat{j} + \frac{1}{2}\hat{k}$ ,  $(1, 2)$ ,  $(2, 0, -1)$  &  $(0, 2, 1)$  is :

(A)  $\pm \frac{1}{\sqrt{6}} (2\hat{i} + \hat{j} + \hat{k})$

(B)  $\frac{1}{\sqrt{6}} (\hat{i} + 2\hat{j} + \hat{k})$

(C)  $\frac{1}{\sqrt{6}} (\hat{i} + \hat{j} + \hat{k})$

(D)  $\frac{1}{\sqrt{6}} (2\hat{i} - \hat{j} - \hat{k})$

29. If ABCD is a parallelogram,

$\vec{AB} = 2\hat{i} + 4\hat{j} - 5\hat{k}$  and

$\vec{AD} = \hat{i} + 2\hat{j} + 3\hat{k}$ , then the unit vector in the direction of BD is :

### QUEST TUTORIALS

- (A)  $\frac{1}{\sqrt{69}}(\hat{i} + 2\hat{j} - 8\hat{k})$  (C)  $15\hat{a} - 7\hat{b}$  (D)  $15\hat{a} + 7\hat{b}$
- (B)  $\frac{1}{69}(\hat{i} + 2\hat{j} - 8\hat{k})$
- (C)  $\frac{1}{\sqrt{69}}(-\hat{i} - 2\hat{j} + 8\hat{k})$
- (D)  $\frac{1}{69}(-\hat{i} - 2\hat{j} + 8\hat{k})$
30. Let  $\vec{b} = 3\hat{j} + 4\hat{k}$ , and let  $\vec{b}_1$  and  $\vec{b}_2$  be component vectors of  $\vec{b}$  parallel and perpendicular to  $\vec{a}$ . If  $\vec{a} = \frac{3}{2}\hat{i} + \frac{3}{2}\hat{j}$ , then  $\vec{b}_2 =$
- (A)  $\frac{3}{2}\hat{i} + \frac{3}{2}\hat{j} + 4\hat{k}$
- (B)  $-\frac{3}{2}\hat{i} + \frac{3}{2}\hat{j} + 4\hat{k}$
- (C)  $-\frac{3}{2}\hat{i} + \frac{3}{2}\hat{j}$  (D) None of these
31. If the points whose position vectors are  $3\hat{i} - 2\hat{j} - \hat{k}$ ,  $2\hat{i} + 3\hat{j} - 4\hat{k}$ ,  $-\hat{i} + \hat{j} + 2\hat{k}$  and  $4\hat{i} + 5\hat{j} + \lambda\hat{k}$  lie on a plane, then  $\lambda =$
- (A)  $-\frac{146}{17}$  (B)  $-\frac{146}{17}$
- (C)  $-\frac{146}{17}$  (D)  $-\frac{146}{17}$
32. A and B are two points. The position vector of A is  $6\vec{b} - 2\vec{a}$ . A point P divides the line AB in the ratio 1 : 2. If  $\vec{p}$  is the position vector of P, then the position vector of B is given by :
- (A)  $7\hat{a} - 15\hat{b}$  (B)  $7\hat{a} + 15\hat{b}$
- (C)  $15\hat{a} - 7\hat{b}$  (D)  $15\hat{a} + 7\hat{b}$
33. If  $\vec{a}$  &  $\vec{b}$  are unit vectors making an angle  $\theta$  with each other then  $|\vec{a} - \vec{b}|$  is :
- (A) 1 (B) 0
- (C)  $\cos \frac{\theta}{2}$  (D)  $2 \sin \frac{\theta}{2}$
34. If the vectors,  $\vec{a}, \vec{b}, \vec{c}$ ,  $\hat{i} + b\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} + c\hat{k}$  ( $a \neq b \neq c \neq 1$ ) are coplanar, then the value of,  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} =$
- (A) -1 (B)  $-\frac{1}{2}$
- (C) 0 (D) 1
35. If C is the middle point of AB and P is any point outside AB, then :  $\vec{PA} + \vec{PB} = PC$
- (A)  $\vec{PA} + \vec{PB} = 2\vec{PC}$
- (B)  $\vec{PA} + \vec{PB} = 2\vec{PC}$
- (C)  $\vec{PA} + \vec{PB} + \vec{PC} = 0$
- (D)  $\vec{PA} + \vec{PB} + 2\vec{PC} = 0$
36.  $\vec{a}, \vec{b}, \vec{c}$  are three non-zero, non-coplanar vectors and  $\vec{p}, \vec{q}, \vec{r}$  are three other vectors such that,
- $\vec{p} = \frac{\vec{b} \times \vec{c}}{\vec{a} \cdot \vec{b} \times \vec{c}}$ ,  $\vec{q} = \frac{\vec{c} \times \vec{a}}{\vec{a} \cdot \vec{b} \times \vec{c}}$  and
- $\vec{r} = \frac{\vec{a} \times \vec{b}}{\vec{a} \cdot \vec{b} \times \vec{c}}$ , then  $[\vec{p}, \vec{q}, \vec{r}]$  equals

## QUEST TUTORIALS

- (A)  $\vec{a} \cdot \vec{b} \times \vec{c}$  (B)  $\frac{1}{\vec{a} \cdot \vec{b} \times \vec{c}}$   
 (C) 0 (D) None of these
37. Let  $\vec{a} = 2\hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + \hat{j} - 2\hat{k}$  &  $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$  be three vectors. A vector in the plane of  $\vec{b}$  &  $\vec{c}$  whose projection on  $\vec{a}$  is of magnitude is :
- (A)  $2\hat{i} - 3\hat{j} + 3\hat{k}$  (B)  $2\hat{i} + 3\hat{j} + 3\hat{k}$   
 (C)  $-2\hat{i} - \hat{j} + 5\hat{k}$  (D)  $2\hat{i} + \hat{j} + 5\hat{k}$
38. The magnitudes of mutually perpendicular forces  $\vec{a}$ ,  $\vec{b}$  &  $\vec{c}$  are 2, 10 and 11 respectively. Then the magnitude of its resultant is :
- (A) 12 (B) 15  
 (C) 9 (D) None of these
39. A vector  $\vec{a}$  has components  $2p$  &  $1$  with respect to a rectangular cartesian system. The system is rotated through a certain angle about the origin in the anti-clockwise sense. If  $\vec{a}$  has components  $p + 1$  &  $1$  w.r.t. the new system, then :
- (A)  $p = 0$  (B)  $p = 1$  or  $-\frac{1}{3}$   
 (C)  $p = -1$  or  $-\frac{1}{3}$  (D)  $p = 1$  or  $-1$
40. Let the value of  $\vec{a} \cdot \vec{b} \times \vec{c}$  be  $3$  and  $\vec{b} \cdot \vec{c} \times \vec{a} = 2$ , then the value of  $\vec{c} \cdot \vec{a} \times \vec{b}$  is :
- (A)  $1$  (B)  $2$   
 (C)  $3$  (D)  $4$
41. If  $(x, y, z) \neq (0, 0, 0)$  and  $(\hat{i} + \hat{j} + 3\hat{k})x + (3\hat{i} - 3\hat{j} + \hat{k})y + (-4\hat{i} + 5\hat{j})z = \lambda(x\hat{i} + y\hat{j} + z\hat{k})$ , then the value of  $\lambda$  will be :
- (A)  $-2, 0$  (B)  $0, -2$   
 (C)  $-1, 0$  (D)  $0, -1$
42. If three non-zero are,  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ . If  $\vec{d}$  is the unit vector perpendicular to the vectors  $\vec{a}$  &  $\vec{b}$  and the angle between  $\vec{a}$  &  $\vec{c}$  is  $\frac{\pi}{6}$ , then  $\vec{d} \cdot \vec{c}$  is equal to :
- (A) 0 (B)  $\frac{3(\sum a_i^2)(\sum b_i^2)(\sum c_i^2)}{4}$   
 (C) 1 (D)  $\frac{(\sum a_i^2)(\sum b_i^2)}{4}$
43. The position vector of coplanar points A, B, C, D are respectively in such a way that,  $(\vec{a} - \vec{d}) \cdot (\vec{b} - \vec{c}) = (\vec{b} - \vec{d}) \cdot (\vec{c} - \vec{a}) = 0$ , then the point D of the  $\Delta ABC$  is :
- (A) Incentre (B) Circumcentre

### QUEST TUTORIALS

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- (C) Orthocentre (D) None of these
44. If  $\vec{F}_1 = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{F}_2 = 2\hat{i} + \hat{j} - \hat{k}$ , and  $\vec{F}_3 = \hat{i} + \hat{j} + \hat{k}$ , then the scalar product of  $\vec{F}_1$  and  $\vec{AB}$  will be :  
 (A) 3 (B) 6  
 (C) 9 (D) 12
45. If the moduli of the vectors,  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are 3, 4, 5 respectively and  $\vec{a}$  &  $\vec{b} + \vec{c}$ ,  $\vec{b}$  &  $\vec{c} + \vec{a}$ ,  $\vec{c}$  &  $\vec{a} + \vec{b}$  are mutually perpendicular, then the modulus of  $\vec{a} + \vec{b} + \vec{c}$  is :  
 (A)  $\sqrt{12}$  (B) 12  
 (C)  $5\sqrt{2}$  (D) 50
46. If the moduli of  $\vec{a}$  &  $\vec{b}$  are equal and angle between them is  $120^\circ$  and  $\vec{a} \cdot \vec{b} = -8$ , then  $|\vec{a} + \vec{b}|$  is equal to :  
 (A) -5 (B) -4  
 (C) 4 (D) 5
47. If  $\vec{a} = (1, a, a^2)$ ,  $\vec{b} = (1, b, b^2)$  and  $\vec{c} = (1, c, c^2)$  are non-coplanar vectors, then  $abc$  is equal to :  
 (A) -1 (B) 0  
 (C) 1 (D) 4
48. If three vectors,  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + \hat{j} - \hat{k}$  &  $\vec{c} = \hat{i} - \hat{j} + \hat{k}$  represents a cube, then its volume will be :  
 (A) 616 (B) 308  
 (C) 154 (D) None of these
49. If  $\vec{a}$  &  $\vec{b}$  are two vectors, then  $(\vec{a} \times \vec{b})^2$  equals :  
 (A)  $\begin{vmatrix} \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{a} \\ \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{a} \end{vmatrix}$  (B)  $\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} \end{vmatrix}$   
 (C)  $\begin{vmatrix} \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} \end{vmatrix}$  (D) None of these
50. The position vector of vertices of a  $\Delta ABC$  are  $4\hat{i} - 2\hat{j}$ ,  $\hat{i} + 4\hat{j} - 3\hat{k}$  and  $-\hat{i} + 5\hat{j} + \hat{k}$  respectively. Then angle  $\angle C$  is equal to :  
 (A)  $30^\circ$  (B)  $45^\circ$   
 (C)  $60^\circ$  (D)  $90^\circ$
51. If  $\vec{a}$  &  $\vec{b}$  are unit vectors and  $\vec{a} - \vec{b}$  is also a unit vector, then the angle between  $\vec{a}$  &  $\vec{b}$  is :  
 (A)  $\frac{\pi}{4}$  (B)  $\frac{\pi}{3}$   
 (C)  $\frac{\pi}{2}$  (D)  $\frac{2\pi}{3}$
52. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = 2\hat{i} - \hat{j} + \hat{k}$  &  $\vec{c} = \hat{i} + \hat{j} - \hat{k}$ , then  $\vec{a} \times (\vec{b} \times \vec{c}) =$   
 (A)  $2\hat{i} + 3\hat{j} - 7\hat{k}$  (B)  $20\hat{i} - 3\hat{j} - 7\hat{k}$   
 (C)  $20\hat{i} + 3\hat{j} - 7\hat{k}$  (D) None of these

### QUEST TUTORIALS

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53. If  $\vec{a}, \vec{b}, \vec{c}$  are coplanar vectors, then

$$(A) \begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{b} & \vec{c} & \vec{a} \\ \vec{c} & \vec{a} & \vec{b} \end{vmatrix} = 0$$

$$(B) \begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \end{vmatrix} = 0$$

$$(C) \begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{c} & \vec{b} \cdot \vec{b} \end{vmatrix} = 0$$

$$(D) \begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{c} & \vec{c} \cdot \vec{b} \end{vmatrix} = 0$$

54. A unit vector which is coplanar to vector,  $\hat{i} + \hat{j} + 2\hat{k}$  and  $\hat{i} + 2\hat{j} + \hat{k}$  and perpendicular to  $\hat{i} + \hat{j} + \hat{k}$ , is :

$$(A) \frac{\hat{i} - \hat{j}}{\sqrt{2}} \quad (B) \pm \left( \frac{\hat{j} - \hat{k}}{\sqrt{2}} \right)$$

$$(C) \frac{\hat{k} - \hat{j}}{\sqrt{2}} \quad (D) \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$$

55. If  $\vec{x} \cdot \vec{a} = 0$ ,  $\vec{x} \cdot \vec{b} = 0$  &  $\vec{x} \cdot \vec{c} = 0$  for some non-zero vector  $\vec{x}$ , then the true statement is :

$$(A) [\vec{a} \vec{b} \vec{c}] = 0 \quad (B) [\vec{a} \vec{b} \vec{c}] \neq 0$$

$$(C) [\vec{a} \vec{b} \vec{c}] = 1 \quad (D) \text{None of these}$$

56. If  $\vec{a}$  has magnitude 5 and points north-east & vector  $\vec{b}$  has magnitude 5 & points north-west, then  $|\vec{a} - \vec{b}|$  is equal to :

$$(A) 25 \quad (B) 5$$

$$(C) 7 \quad (D) 5\sqrt{2}$$

57. In a regular hexagon ABCDEF,  $\vec{AE}$  is equal to :

$$(A) \vec{AC} + \vec{AF} + \vec{AB} \quad (B) \vec{AC} + \vec{AF} - \vec{AB}$$

$$(C) \vec{AC} + \vec{AB} - \vec{AF} \quad (D) \text{None of these}$$

58.  $\vec{OD} + \vec{DA} + \vec{DB} + \vec{DC} =$

$$(A) \vec{OA} + \vec{OB} + \vec{OC} \quad (B) \vec{OA} + \vec{OB} - \vec{BD}$$

$$(C) \vec{OA} + \vec{OB} + \vec{OC} \quad (D) \text{None of these}$$

59. In a  $\Delta ABC$ , if  $2\sqrt{3}\vec{AC} = 3\sqrt{3}\vec{CB}$ , then  $2\sqrt{3}\vec{OA} + 3\sqrt{3}\vec{OB}$  equals :

$$(A) 5\sqrt{3}\vec{OC} \quad (B) -\sqrt{3}\vec{OC}$$

$$(C) \sqrt{3}\vec{OC} \quad (D) \text{None of these}$$

60. If  $\vec{AO} + \vec{OB} = \vec{BO} + \vec{OC}$ , then A, B, C form :

$$(A) \text{Equilateral triangle}$$

$$(B) \text{Eight angled triangle}$$

$$(C) \text{Isosceles triangle}$$

$$(D) \text{Line}$$

61. If the position vectors of A and B are  $\hat{i} + 3\hat{j} - 7\hat{k}$  and  $5\hat{i} - 2\hat{j} + 4\hat{k}$ , then

#### QUEST TUTORIALS

- the direction cosine of  $\vec{AB}$  along y - axis is :
- (A)  $\frac{4}{\sqrt{162}}$  (B)  $-\frac{5}{\sqrt{162}}$   
 (C) - 5 (D) 11
62. The point B divides the arc AC of a quadrant of a circle in the ratio 1 : 2. If O is the centre and  $\vec{OA} = \vec{a}$  and  $\vec{OB} = \vec{b}$ , then the vector  $\vec{OC}$  is :
- (A)  $\vec{b} - 2\vec{a}$  (B)  $2\vec{a} - \vec{b}$   
 (C)  $3\vec{b} - 2\vec{a}$  (D) None of these
63. The points D, E, F divide BC, CA & AB of the triangle ABC in the ratio 1 : 4, 3 : 2 & 3 : 7 respectively & the point K divides AB in the ratio 1 : 3, then  $(\vec{AD} + \vec{BE} + \vec{CF}) : \vec{CK} =$
- (A) 1 : 1 (B) 2 : 5  
 (C) 5 : 2 (D) None of these
64. If vector  $\vec{a} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and vector  $\vec{b} = 3\hat{i} + 4\hat{j} - 7\hat{k}$ , then  $\vec{a} \cdot \vec{b} =$
- (A)  $\frac{3}{7}$  (B)  $\frac{1}{7}$   
 (C) 3 (D) 7
65. If  $\vec{r}$  be position vector of any point on a sphere &  $\vec{a}$  &  $\vec{b}$  are respectively position vectors of the extremities of a diameter, then :
- (A)  $\vec{r} \cdot (\vec{a} + \vec{b}) = 0$  (B)  $\vec{r} \cdot (\vec{a} - \vec{b}) = 0$   
 (C)  $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = 0$  (D)  $(\vec{r} - \vec{a}) \cdot (\vec{a} - \vec{b}) = 0$
66. If  $\vec{a} \times (\vec{b} \times \vec{c}) = 0$ , then :
- (A)  $\vec{a} \parallel \vec{b}$   
 (B)  $\vec{b} \parallel \vec{c}$   
 (C)  $\vec{a} \parallel \vec{c}$   
 (D)  $\vec{a} \perp \vec{b}$
67. If  $\vec{a}, \vec{b}, \vec{c}$  are three non-coplanar vectors, then  $(\vec{a} + \vec{b} + \vec{c}) \cdot [(\vec{a} + \vec{b}) \times (\vec{a} + \vec{c})] =$
- (A)  $[\vec{a} \vec{b} \vec{c}]$  (B)  $2[\vec{a} \vec{b} \vec{c}]$   
 (C)  $-[\vec{a} \vec{b} \vec{c}]$  (D) 0
68. If  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar unit vectors such that,  $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{b}$  then the angle between  $\vec{a}$  &  $\vec{b}$  is :
- (A)  $\frac{\pi}{4}$  (B)  $\frac{\pi}{2}$   
 (C)  $\frac{3\pi}{4}$  (D)  $\pi$
69. Given  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$  &  $\vec{c} = -\hat{i} + 2\hat{j} - \hat{k}$ . A unit vector perpendicular to both  $\vec{a} + \vec{b}$  &  $\vec{b} + \vec{c}$  is :
- (A)  $\hat{i}$  (B)  $\hat{j}$

### QUEST TUTORIALS

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- (C)  $\hat{k}$  (D)
70. Force  $3\hat{i} + 2\hat{j} + 5\hat{k}$  and  $2\hat{i} + \hat{j} - 3\hat{k}$  are acting on a particle and displace it from the point  $2\hat{i} - \hat{j} - 3\hat{k}$  to the point  $4\hat{i} - 3\hat{j} + 7\hat{k}$ , then work done by the force is :  
 (A) 30 units (B) 36 units  
 (C) 24 units (D) 18 units
71. The point having position vectors,  $2\hat{i} + 3\hat{j} + 4\hat{k}$ ,  $3\hat{i} + 4\hat{j} + 2\hat{k}$  and  $4\hat{i} + 2\hat{j} + 3\hat{k}$  are the vertices of :  
 (A) Right angle triangle  
 (B) Isosceles triangle  
 (C) Equilateral triangle  
 (D) Collinear
72. The distance of the point, B  $(\hat{i} + 2\hat{j} + 3\hat{k})$  from the line which is passing through A  $(4\hat{i} + 2\hat{j} + 2\hat{k})$  and which is parallel to the vector,  $\vec{C} = 2\hat{i} + 3\hat{j} + 6\hat{k}$  is :  
 (A) 10 (B)  
 (C) 100 (D) None of these
73. Given the following simultaneous equations for vectors  $\vec{x}$  &  $\vec{y}$  .  
 $\vec{x} + \vec{y} = \vec{a}$  ..... (i)  
 $\vec{x} \times \vec{y} = \vec{b}$  ..... (ii)  
 $\vec{x} \cdot \vec{a} = 1$  ..... (iii)  
 Then  $\vec{x} = \underline{\hspace{2cm}}$ ,  $\vec{y} = \underline{\hspace{2cm}}$  .
- (A)  $\vec{a}, \vec{a} - \vec{x}$  (B)  $\vec{a} - \vec{b}, \vec{b}$   
 (C)  $\vec{b}, \vec{a} - \vec{b}$  (D) None of these
74. Let  $\alpha, \beta, \gamma$  be distinct real numbers . The points with position vectors,  $\alpha\hat{i} + \beta\hat{j} + \gamma\hat{k}$ ,  $\beta\hat{i} + \gamma\hat{j} + \alpha\hat{k}$  and  $\gamma\hat{i} + \alpha\hat{j} + \beta\hat{k}$  :  
 (A) Are collinear  
 (B) Form an equilateral triangle  
 (C) Form a scalene triangle  
 (D) Form a right angled triangle
75. Let  $\vec{p}$  &  $\vec{q}$  be the position vectors of P & Q respectively with respect to O and  $|\vec{p}| = p, |\vec{q}| = q$ . The points R & S divide PQ internally & externally in the ratio 2 : 3 respectively . If  $\vec{OR}$  and  $\vec{OS}$  are perpendicular, then  
 (A)  $9p^2 = 4q^2$  (B)  $4p^2 = 9q^2$   
 (C)  $4p = 4q$  (D)  $4p = 9q$
76. If  $(\vec{a} \times \vec{b})^2 + (\vec{a} \cdot \vec{b})^2 = 144$  &  $|\vec{a}| = 4$  then  $|\vec{b}| =$   
 (A) 16 (B) 8  
 (C) 3 (D) 12
77. The value of c so that for all real x, the vectors  $x\hat{i} + 2\hat{j} + 2cx\hat{k}$  and  $x\hat{i} + 2\hat{j} + 2cx\hat{k}$  make an obtuse angle are :  
 (A)  $c < 0$  (B)  $0 < c < \frac{4}{3}$   
 (C)  $-\frac{4}{3} < c < 0$  (D)  $c > 0$
78.  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$ ;  $\vec{a} \neq \vec{0}$ ;

## QUEST TUTORIALS

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- $\neq 0$  ;  $\neq \lambda$  , is not perpen. to (A) (B)  $\sqrt{3}$   
 , then = (C) 2 (D)  $\sqrt{5}$
- (A) - (B) +  
 (C)  $\times$  + (D)  $\times$  +

ANSWERS

79. A non-zero vector is parallel to the line of intersection of the plane determined by the vectors, & the plane determined by the vectors,  $\hat{i} - \hat{j}, \hat{i} + \hat{k}$ . The angle between  $\vec{a}$  & the vector is :
- (A)  $\frac{\pi}{4}$  or  $\frac{3\pi}{4}$  (B)  $\frac{2\pi}{4}$  or  $\frac{3\pi}{4}$   
 (C)  $\frac{\pi}{2}$  or  $\frac{3\pi}{2}$  (D) None of these
80. If  $\vec{b}$  &  $\vec{c}$  are any two non-collinear unit vectors and  $\vec{a}$  is any vector, then

1. C 2. B 3. D 4. C 5. B 6. C  
 7. B 8. D 9. B 10. B 11. C 12. D  
 13. C 14. A 15. D 16. D 17. B 18. A  
 19. D 20. B 21. B 22. C 23. A 24. A  
 25. D 26. B 27. A 28. A 29. C 30. B  
 31. A 32. A 33. D 34. D 35. B 36. B  
 37. C 38. B 39. B 40. B 41. D 42. D  
 43. C 44. C 45. C 46. C 47. A 48. D  
 49. B 50. D 51. B 52. A 53. B 54. B  
 55. A 56. D 57. B 58. C 59. A 60. C  
 61. B 62. C 63. B 64. B 65. D 66. B  
 67. C 68. C 69. C 70. C 71. C 72. B  
 73. D 74. B 75. A 76. C 77. C 78. B  
 79. A 80. A 81. B 82. B

$$= \frac{(\vec{a} \cdot \vec{b})\vec{c} + (\vec{a} \cdot \vec{c})\vec{b}}{|\vec{b} \times \vec{c}|}$$

- (A)  $\vec{a}$  (B)  
 (C) (D) 0
81. The value of x for which the angle between the vectors,  
 and is acute & the angle between  $\vec{b}$  and x - axis lies between  $\pi/2$  and  $\pi$  satisfy :
- (A)  $x > 0$  (B)  $x < 0$   
 (C)  $x > 1$  only (D)  $x < -1$  only
82. If the sum of two unit vectors is a unit vector, then the magnitude of their difference is :

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